

$$8.89. a) 2 \sin^3 x - 3 \sin x \cos x = 0 \quad \sin^2 x + \cos^2 x = 1$$

$$\sin^2 x = 1 - \cos^2 x$$

$$\sin x (2 \sin^2 x - 3 \cos x) = 0$$

$$\sin x = 0 \quad \vee \quad 2 \sin^2 x - 3 \cos x = 0$$

$$\underline{x = k \cdot \pi}$$

$$2(1 - \cos^2 x) - 3 \cos x = 0$$

$$-2 \cos^2 x - 3 \cos x + 2 = 0 \quad | \cdot (-1)$$

$$2 \cos^2 x + 3 \cos x - 2 = 0 \quad \text{podstawiamy } \cos x = t$$

$$2t^2 + 3t - 2 = 0 \quad a=2, b=3, c=-2 \quad t \in \langle -1; 1 \rangle$$

$$\Delta = b^2 - 4ac = 3^2 - 4 \cdot 2 \cdot (-2) = 9 + 16 = 25 \quad \sqrt{\Delta} = 5$$

$$t_1 = \frac{-b - \sqrt{\Delta}}{2a} = \frac{-3 - 5}{2 \cdot 2} = \frac{-8}{4} = -2 \notin \langle -1; 1 \rangle$$

$$t_2 = \frac{-b + \sqrt{\Delta}}{2a} = \frac{-3 + 5}{2 \cdot 2} = \frac{2}{4} = \frac{1}{2}$$

$$\cos x = \frac{1}{2}$$

$$x = \pm \frac{\pi}{3} + 2k\pi$$

odp:

$$\begin{cases} x = k \cdot \pi \\ x = \pm \frac{\pi}{3} + 2k\pi, \end{cases} \quad k \in \mathbb{C}$$